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## **Calculus of variations**

## **Euler-Lagrange equation**

```
$q$
                                                                                                                                                                                                                                                                                                                                                                                          $S$
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          $q\left(t\right)$
                                                                                                                                                                                      $S$
\begin{equation} \displaystyle S(q) = \int a^b L(t,q(t),q'(t))\ \mathrm{d}t \end{equation}
                             $q$
\left(a \right) q \cdot a = q(t) 
                                                                                                                                            가
                                                                                                                                                                                                                                              , q\left(a\right) = x a, q\left(b\right) = x b
                                                    $q$
                              • $q'$
                                                                                                   $q$
 1
                                    $f$ 가,
                                                                                                                                                                                 f(a\cdot y) = c, f(b\cdot y) = d
                     $J$
가
                                                    $F$가
                                                                                                                                                                                                                                                                                                                              가
                                                                                                                                                                                                                                                                                                                                                                                          . (가
                                                                                                                                        .)
                                     $f$가
                                                                                                                                                                                                                                                                                                                                                                          , $f$
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           가
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               , $J$
                                                                                                                                                                                         ) $J$
                ($f$가 $J$
                                                                                                                                                                                                                                                                                                                                                              .($f$가 $J$
                                                     $f$
                                                                                                                                                                                                                                                                                     q \exp \sinh(x \cdot y) =
f\left(x\right)+\epsilon\eta\left(x\right)$
                                                                                                                                                                                                                                                                                                                                                                                                                                       $\eta\left(x\right)$
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   \left( b\right) = 0
                                                                                                                                                                                                                                                                                     가
                                                                                                                                                                                                                                                                                                                                                                                                                                                , $f$
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          $g$
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 $J$
                                가
\beta = \frac{a^b F(x,g \epsilon(x), g \vee x)}{\| \cdot \|_{x,y}} 
                                     $1$
                                                                                    $\epsilon$
\ensuremath{\mbox{begin}\{\ensuremathrm{d} J}{\mbox{mathrm{d} \varepsilon} = \int_a^b}
\frac{d}F}{\mathbf{d}F}_{\mathbf{d}}(x,g \vee x,g \vee x
```

x{\partial x}{\partial \varepsilon} + \frac{\partial F}{\partial g \varepsilon}\frac{\partial}  $\verb|g| \arepsilon| {\partial $$\partial $$F} {\partial $g'_\arepsilon} \\$  $g' \vee F(x) = \frac{F}{\rho(x)} + \frac{F}{\rho(x)}$ \frac{\partial F}{\partial g\_\varepsilon'}. \end{equation}

 $\beta = \inf a^b \left( x \right)$ F{\partial g \varepsilon} + \eta'(x) \frac{\partial F}{\partial g \varepsilon'} \, \right]\, dx. \end{equation}

 $\left( \frac{F}{\phi} \right) = \int a^b \left( \frac{F}{\phi} \right) f(x)$ F {\partial f'} \,\right]\,dx = 0. \end{equation}

 $\beta = \int a^b \left[ \frac{F}{\phi f(a)} - \frac{d}{dx} \right]$ F {\partial f'} \right] \eta(x)\,dx + \left[ \eta(x) \frac{\partial F} {\partial f'} \right] a^b. \end{equation}

\$\eta\$

 $\left( F_{\alpha } \right) = \int_{\alpha } \left( F_{\alpha } F_{\alpha } \right)$ F {\partial f'} \right] \eta(x)\,dx. \,\! \end{equation}

\begin{equation}  $0 = \frac{F}{\mathbf{F}} - \frac{d}{dx} \frac{F}{\mathbf{F}}.$ \end{equation}

가

 $\begin{equation} L | f(x)^2 | + f'(x)^2 |, dx \leq (equation) \\$ 

$$f$$
 \$f\left(a\right) = y\_a, f\left(b\right)=y\_b\$

\$f\$

 $\left(\frac{d}{dx}\right)^2 = -\left(\frac{d}{dx}\right)^2$ \end{equation}

 $\ensuremath{\mbox{begin}\{\mbox{equation} \begin{matrix} 0 \&=\& \frac{d}{dx}\frac{\partial }{\partial }'}\$ \end{matrix} \end{equation}

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0

가 , \$f'\left(x\right)\$

 $\left( \left( x\right) =C\right) =C$ 

가  $f\left(x\right) = Cx + D$ \$

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